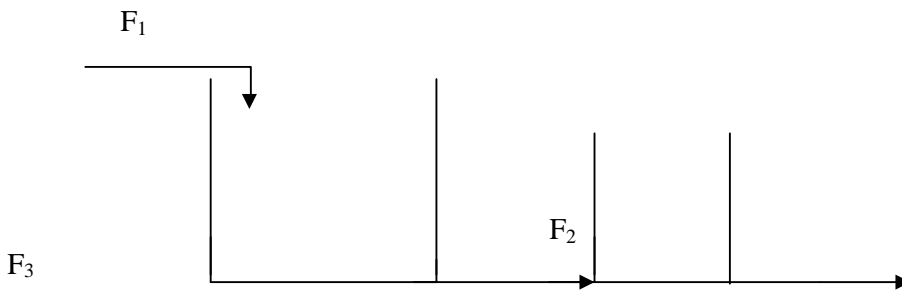
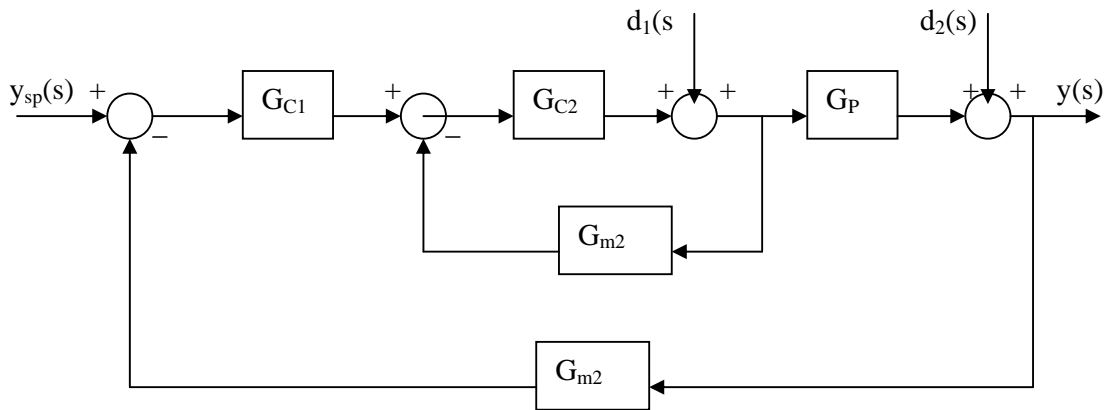


**(Design)**

1. Problem IV.2 in the textbook (Chemical Process control by G. Stephanopoulos).
2. Consider the two interacting tanks shown in the figure. We want to control the liquid level  $h_2$  of tank 2 by manipulating flow rate  $F_1$  through a proportional controller. Assume that tank 1 has a cross-sectional area of  $5 \text{ ft}^2$ ; while for tank 2 the cross-sectional area is  $2 \text{ ft}^2$ . Initially, the system is at steady state with  $F_1 = 1 \text{ ft}^3/\text{min}$ ,  $h_1 = 4 \text{ ft}$ , and  $h_2 = 3 \text{ ft}$ . Find the values of the controller gain that produce
  - a- A critically damped response, or
  - b- An underdamped response with decay ratio equal to  $1/4$  for  $h_2$ .
  - c- For each of the two cases above, describe the dynamic response of liquid level  $h_1$  in tank 1 for a unit step change in the set point of  $h_2$ . Sketch qualitatively these two responses.



3. Consider the block diagram Shown below, which includes two control loops.



Assume  $G_{m1} = G_{m2} = 1$  and  $G_p = 10/[(s+1)(2s+1)]$

- a) Derive an expression for the closed-loop response to a unit step change in the set point, assuming that both controllers are proportional with  $K_{c1}$  and  $K_{c2}$ .
- b) Examine if the closed-loop response exhibits an offset to a unit step change in the set point. If it does, compute the value of the offset. If it does not, explain why.
- c) Suppose that  $K_{c2} = 1$ . Find the values of  $K_{c1}$  which produces (1) a critically damped response, and (2) an underdamped response with a decay ratio  $1/4$ .
- d) Sketch the closed-loop response for each of the two cases in part (c).
- e) Compute the closed-loop poles for the two cases in part (c). What do you observe?